

If b , h and r are lengths, which of these calculate an area: $2bh$, r^2h , $3b + 2r$, $b(h + r)$, π^2b , $\frac{3b^2+r^2}{h}$?

$$\frac{2bh}{b(h+r)}$$

What is the formula for the total surface area of a closed cylinder with base radius r and height h ?

$$A = \pi r^2 h + 2\pi r^2$$

When would you use the sine rule?

In non-right angled triangles, the sine rule involves two angles and their opposite sides.

$$\frac{a}{\sin A} = \frac{b}{\sin B} \left(= \frac{c}{\sin C} \right)$$

When would you use the cosine rule?

In non-right angled triangles, the cosine rule involves all three sides and one angle.

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Describe the graph given by the equation $x^2 + y^2 = 9$.

Circle; centre (0,0); radius 3

Give the equation of a circle with centre (0,0) and radius $\sqrt{5}$.

$$x^2 + y^2 = 5$$

How can you tell if two vectors are parallel?

One is a multiple of the other

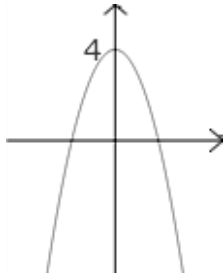
e.g. $\begin{pmatrix} 2 \\ 8 \end{pmatrix}$ and $\begin{pmatrix} 4 \\ 16 \end{pmatrix}$

How do you calculate the magnitude of a vector?

Using Pythagoras' theorem

(Vectors are given in horizontal and vertical components.)

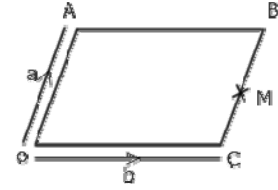
Sketch the parabola $y = 4 - x^2$



$-x^2$ gives the shape of the curve
4 gives the y-intercept

OABC is a parallelogram. M is the midpoint of BC. $\vec{OA} = \mathbf{a}$ and $\vec{OC} = \mathbf{b}$.
Find: a) \vec{OB} b) \vec{AC} c) \vec{MA} .

- a) $\vec{OB} = \mathbf{a} + \mathbf{b}$
b) $\vec{AC} = \mathbf{b} - \mathbf{a}$
c) $\vec{MA} = \frac{1}{2}\mathbf{a} - \mathbf{b}$



Describe the transformation which maps $y = f(x)$ onto $y = f(x) + a$.

Translation, vector $\begin{pmatrix} 0 \\ a \end{pmatrix}$

Describe the transformation which maps $y = f(x)$ onto $y = f(x + a)$.

Translation, vector $\begin{pmatrix} -a \\ 0 \end{pmatrix}$

Describe the transformation which maps $y = f(x)$ onto $y = -f(x)$.

Reflection in the x -axis

Describe the transformation which maps $y = f(x)$ onto $y = f(-x)$.

Reflection in the y -axis

Describe the transformation which maps $y = f(x)$ onto $y = af(x)$.

Vertical stretch, scale factor a

Describe the transformation which maps $y = f(x)$ onto $y = f(ax)$.

Horizontal stretch, scale factor $1/a$

Describe the transformation which maps $y = \sin x$ onto $y = 2 \sin x$

Vertical stretch, scale factor 2

Describe the three transformations needed to map $y = \cos x$ onto $y = 4 - 2 \cos 3x$.

Vertical stretch, scale factor 2
 Horizontal stretch; scale factor $1/3$
 Translation, vector $\begin{pmatrix} 0 \\ 4 \end{pmatrix}$

The four cards below contain more complex puzzles, which require more working (all using GCSE Maths skills). You may wish to use them separately as a starter, plenary, discussion exercise or homework task.

Extension: Find an expression for the difference in area between a circle with radius r and the square it contains.

Circle radius = square diagonal
 Using Pythagoras, square side = $r\sqrt{2}$

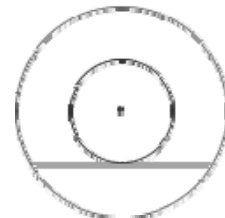
$$\begin{aligned} \text{Area difference} &= \pi r^2 - (r\sqrt{2})^2 \\ &= r^2(\pi - 2) \end{aligned}$$

Extension: In a circle, a chord measuring 2m is also a tangent of a smaller concentric circle. Find the area of the ring between the two circles.

Call the large circle a and the small circle b .

Using Pythagoras:

$$\begin{aligned} r_a^2 &= 1 + r_b^2 \\ A &= \pi(1 + r_b^2) - \pi r_b^2 \\ &= \pi \text{ metres} \end{aligned}$$



Extension: The volumes of two spheres are 5cm^3 and 135cm^3 . State the ratio of their:
 a) radii b) diameters c) surface areas.

Ratio of volumes = 1 : 27, so ...

- a) ratio of radii = 1 : 3
- b) ratio of diameters = 1 : 3
- c) ratio of surface areas = 1 : 9.

Extension: Calculate the area of a right angled triangle where: $a = (x - 2)$, $b = (x + 5)$, hypotenuse = $(2x - 1)$.

Using Pythagoras:

$$\begin{aligned} (2x - 1)^2 &= (x - 2)^2 + (x + 5)^2 \\ x &= 7 \text{ (cannot be -2)} \end{aligned}$$

$$\text{Area} = \frac{1}{2}(7 - 2)(7 + 5) = 30 \text{ sq. units}$$