



Solutions

The line intercepts the curve at (1, 8) and (4, 5)

$$\text{Shaded area} = \int_1^4 (-x^2 + 4x + 5) dx - \left(\frac{8+5}{2}\right) \times 3 = 24 - \frac{39}{2} = \frac{9}{2} \text{ square units}$$

$$\text{Segment area} = \frac{1}{2} \times 8^2 \times \frac{\pi}{6} - \frac{1}{2} \times 8^2 \times \sin\left(\frac{\pi}{6}\right) = 32 \left(\frac{\pi}{6} - \frac{1}{2}\right) \text{ cm}^2$$

$BC = 10$ cm [cosine rule]

$$\text{Triangle area} = \frac{1}{2} \times 5 \times 10 \times \sin\left(\frac{\pi}{3}\right) = \frac{25\sqrt{3}}{2} \text{ cm}^2$$

Alternatively, angle $ABC = \frac{\pi}{6}$ by the sine rule and therefore angle $BAC = \frac{\pi}{2}$ and since the triangle is right-angled, the area is $\frac{1}{2} \times 5 \times 5\sqrt{3} = \frac{25\sqrt{3}}{2} \text{ cm}^2$